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*Acta Cryst.* (1991). **A47**, 851

**The densest packing of equal circles on a sphere. Erratum.** By D. A. KOTTWITZ, 2152 Hudson Ave., Richland, WA 99352, USA

(Received 29 August 1991)

**Abstract**

Two of the literature references for the paper by Kottwitz [*Acta Cryst.* (1991). **A47**, 158–165] are corrected. In Table 1 (p. 161), the entry for  $n = 19$  should read Lazić, Šenk &

Šeškar (1987), while that for  $n = 23$  should read Tarnai & Gáspár (1990).

All relevant information is given in the *Abstract*.

*Acta Cryst.* (1991). **A47**, 851–852

**Madelung numbers for the theoretical structure type with mutual trigonal prismatic coordination.** By J. ZEMANN, Institut für Mineralogie und Kristallographie, Universität Wien, Dr-Karl-Lueger-Ring 1, A-1010 Wien, Austria

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**Abstract**

Madelung numbers  $\alpha$  are presented for the theoretical *AB* structure type with mutual trigonal prismatic coordination as a function of the deformation leaving the lengths of the *AB* distances in the  $AB_6 (=BA_6)$  prism equal.  $\alpha$  is always smaller than  $\alpha$  (NaCl) and its maximum value is also slightly smaller than the maximum value of  $\alpha$  (NiAs).

The Madelung numbers  $\alpha$  for the NaCl structure type and for the NiAs structure type have been known for a long time (see e.g. Emersleben, 1953/54; Zemmann, 1958). The NaCl type has a mutual octahedral six coordination, while in the NiAs type the Ni atoms are coordinated to six As atoms in the form of an elongated or compressed octahedron and the As atoms to six Ni atoms in the form of a trigonal prism. Theoretically, there also exists an *AB* structure type with mutual trigonal prismatic coordination. Its Madelung numbers  $\alpha$  seem not to have been published as yet.

The crystallographic description of this structure type may be seen in Table 1. The atomic arrangement is closely related to the hexagonal closest packing of spheres: consecutive layers parallel to (00.1) are occupied by *A* and *B* ions, respectively, and a deformation along the *z* axis is allowed. With  $A-B=1$  there is one degree of freedom, for which the angle  $\mu$  between the *AB* direction in the trigonal prism and the *z* axis was chosen. From the point of view of the stereochemistry of ionic compounds only the region of  $\mu$  with  $\arcsin(1/3^{1/2}) \approx 35.26^\circ \leq \mu \leq \arccos(1/2) = 60^\circ$  is of interest. Outside this range some *AA* ( $=$  *BB*) distances are shorter than the *AB* distance in the trigonal prismatic coordination. It should be noted that

Table 1. Theoretical *AB* structure type with mutual trigonal prismatic coordination

Space group:  $P\bar{6}m2 - D_{3h}^1$  (No. 187).

Positions: 1*A* on 1(*c*) 1/3, 2/3, 0; 1*B* on 1(*d*) 2/3, 1/3, 1/2.  $A-B=1$ ;  $\mu$  = angle of *A-B* with the *z* direction ( $\mu < 90^\circ$ ).  $a = 3^{1/2} \sin \mu$ ,  $c = 2 \cos \mu$ ;  $V = 3 \times 3^{1/2} \sin^2 \mu \cos \mu$ .

$\mu$	<i>a</i>	<i>c</i>	<i>V</i>	$\alpha$
35.264390*	1.000000	1.632993	1.414214	1.235585
40.000000	1.113341	1.532089	1.644640	1.506440
45.000000	1.224745	1.414214	1.837117	1.656998
49.106605†	1.309307	1.309307	1.943817	1.712437
50.000000	1.326828	1.285575	1.960006	1.717955
51.000000	1.346056	1.258641	1.974963	1.721567
52.000000	1.364875	1.231323	1.986498	1.722523
53.000000	1.383277	1.203630	1.994537	1.720843
54.000000	1.401259	1.175571	1.999014	1.716516
54.735610‡	1.414214	1.154701	2.000000	1.716160
55.000000	1.418813	1.147153	1.999872	1.709493
60.000000§	1.500000	1.000000	1.948557	1.629560

\*  $\mu = \arcsin(1/3^{1/2})$ ; (*A+B*) form hexagonal closest packing.

†  $\mu = \arctan(2/3^{1/2})$ ; case for which  $a = c$ .

‡  $\mu = \arccos(1/3^{1/2})$ ; case for which *V* has maximum value.

§  $\mu = \arccos(1/2)$ ; case for which  $A-A (=B-B)$  parallel to *z* equals  $A-B (=1)$ .

this structure type can also be conveniently described in the black-white space group  $P6_3'/mmc'$ , No. 267, of the hexagonal system (Shubnikov & Belov, 1964).

Table 1 presents the variation of the lattice parameters, the cell volume and the Madelung number  $\alpha$  as a function of  $\mu$ . The maximum value of the Madelung number [ $\alpha = 1.7226(1)$ ] occurs at  $\mu = 51.8(1)^\circ$ . This  $\mu$  value is clearly different from that at which the cell volume reaches its maximum ( $\mu = 54.74^\circ$ ), but very close to the value at which

an isolated  $AB_6$  complex with symmetry  $\bar{6}2m$  has its electrostatic optimum [ $\mu = 51.6 (1)^\circ$ ].

The maximum  $\alpha$  value of the structure type under consideration is not only definitely smaller than that of the NaCl type ( $\alpha = 1.7476$ ), but also slightly smaller than the maximum value for the NiAs type, *i.e.*  $\alpha = 1.733 (1)$  as derived from the values given by Zemmann (1958). It is, therefore, no surprise that the  $AB$  structure type with mutual trigonal prismatic coordination has no representatives among ionic structures.

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**Quasiperiodic tilings with low-order rotational symmetry. Erratum.** By D. S. CLARK and E. R. SURYANARAYAN, *Department of Mathematics, University of Rhode Island, Kingston, RI 02881, USA*

(Received 20 September 1991)

#### Abstract

Figs. 10(a), (b) of the paper by Clark & Suryanarayan [*Acta Cryst.* (1991), **A47**, 498–502] reproduced poorly. Revised figures with better contrast are here published.

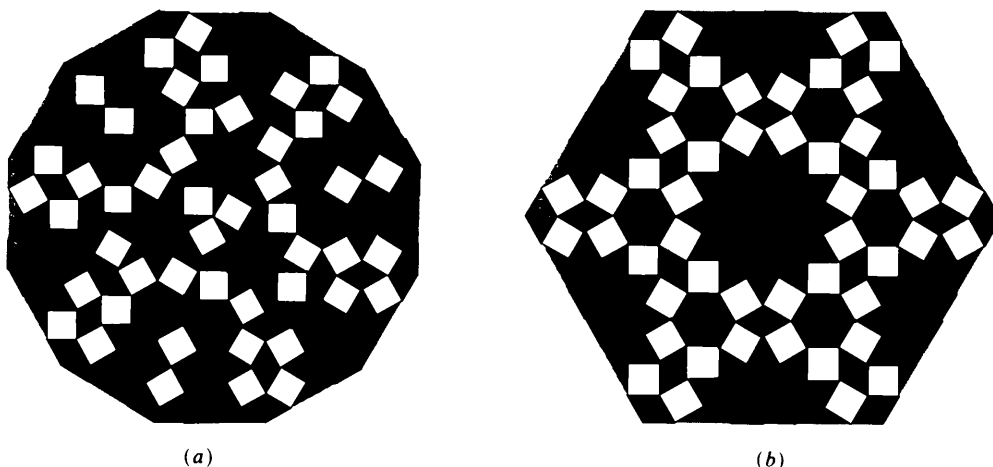


Fig. 10. (a) 3-fold rotational symmetry, 2nd generation. (b) 6-fold rotational symmetry, 2nd generation.

### International Union of Crystallography

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